

## Integration by computer with Mathematica.

### □ Calculus 153/22 M. Pergler April 1999

(this does the same math as the Maple handout, just using a different program so you see the difference in input syntax. Main differences: (a) Function names are capitalized (b) arguments have square brackets (c) You don't have to do the layout (brackets and shading)...*Mathematica* did that.)

```
f[x_] := (2 x^4 - 8 x^3 - 20 x^2 + 216 x - 286) /
          (x^5 - 11 x^4 + 58 x^3 - 134 x^2 + 21 x + 225)
```

```
Integrate[f[x], x]
```

$$-\frac{2}{-3+x} - \frac{1}{2} \operatorname{ArcTan}\left[\frac{4}{-3+x}\right] + \operatorname{Log}[-3+x] - \operatorname{Log}[1+x] + \operatorname{Log}[25-6x+x^2]$$

```
Apart[f[x]]
```

$$\frac{2}{(-3+x)^2} + \frac{1}{-3+x} - \frac{1}{1+x} + \frac{2(-2+x)}{25-6x+x^2}$$

```
g[x_] := (Sin[x] + Tan[Sqrt[x]]) (1 + Exp[1/x])
```

```
Integrate[g[x], {x, 1, 2}]
```

$$\int_1^2 \left(1 + E^{\frac{1}{x}}\right) \left(\sin[x] + \tan[\sqrt{x}]\right) dx$$

```
N[%, 50]
```

```
11.96846920512586
```

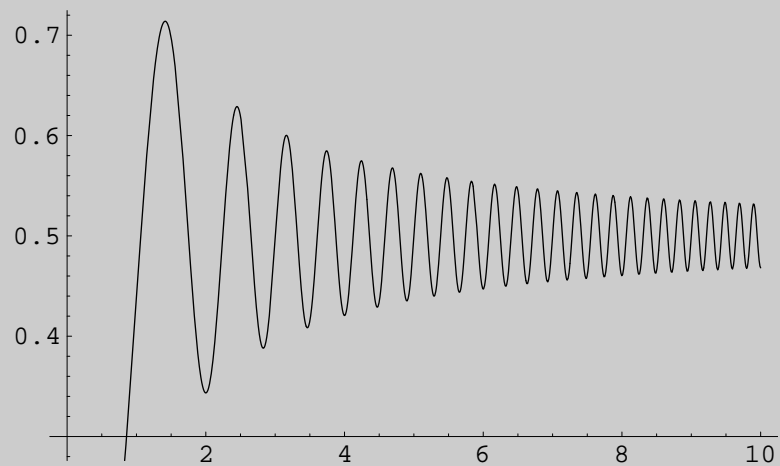
```
Integrate[Sin[x^2], x]
```

$$\sqrt{\frac{\pi}{2}} \operatorname{FresnelS}\left[\sqrt{\frac{2}{\pi}} x\right]$$

Looking up FresnelS in the help browser....

- $\operatorname{FresnelS}[z]$  is given by  $\int_0^z \sin(\pi t^2 / 2) dt$ .
- $\operatorname{FresnelS}[z]$  is an entire function of  $z$  with no branch cut discontinuities.

```
Plot[FresnelS[x], {x, 0, 10}]
```



```
<< Graphics`Polyhedra`
```

```
Show[Truncate[  
  Polyhedron[Dodecahedron], .4]]
```

